

# All Things Algebra®

# PRE-CALCULUS CURRICULUM

## Unit 1: Fundamental Skills

- Laws of Exponents
- Polynomial Operations
- Factoring Polynomials
- Rational Expressions
- Complex Fractions
- Radicals
- Rational Exponents
- Complex Numbers
- Linear & Absolute Value Equations
- Quadratic Equations
- Rational Equations
- Inequalities: Set Builder and Interval Notation
- Linear & Absolute Value Inequalities

## Unit 2: Functions & Their Graphs

- Functions
- Evaluating Functions
- Domain, Range
- Critical Points, Intercepts, Zeros
- Tests for Symmetry; Even and Odd Functions
- Continuity; Types of Discontinuity
- End Behavior
- Average Rate of Change
- Parent Functions
- Transformations
- Graphing Functions
- Function Operations
- Composition of Functions
- Piecewise Functions
- Inverse Relations & Functions

## Unit 3: Polynomial & Rational Functions

- Graphing Power Functions & Identifying Characteristics (includes integral and rational exponents)
- Graphing Polynomial Function & Identifying Characteristics
- Zeros, Linear Factors, Multiplicity
- Dividing Polynomials (Long and Synthetic)
- The Remainder and Factor Theorems
- Rational Zero Theorem
- Descartes' Rule
- Fundamental Theorem of Algebra
- Using Zeros to Write Polynomial Functions
- Graphing Rational Functions
- Nonlinear Inequalities

## Unit 4: Exponential & Logarithmic Functions

- Graphing Exponential Functions
- The Natural Exponential Function
- Logarithms (Evaluating & Change of Base)
- Graphing Logarithmic Functions
- Natural Logarithms
- Properties of Logarithms
- Expanding & Condensing Logarithms
- Exponential Equations
- Logarithmic Equations
- Exponential Growth and Decay Applications
- Logistic Growth Function
- Compound Interest
- Regression (Exponential, Power, Logistic, Logarithmic)

### Unit 5: Trigonometric Functions

- Standard Form of an Angle
- Degrees & Radians; Coterminal Angles
- Degree- Minute-Second Form
- Arc Lengths & Area of Sectors
- Circular Motion (Linear and Angular Speed)
- Trigonometric Functions:  $\sin$ ,  $\cos$ ,  $\tan$
- Reciprocal Functions:  $\csc$ ,  $\sec$ ,  $\cot$
- Right Triangle Trigonometry
- Reference Angles & The Unit Circle
- Law of Sines and Law of Cosines
- Graphs of Sine and Cosine Functions
- Graphs of Tangent Functions
- Graphs of Reciprocal Functions
- Vertical and Phase Shifts of Trigonometric Functions
- Graphs of Inverse Trigonometric Functions
- Compositions of Trigonometric Functions

### Unit 6: Trigonometric Identities & Equations

- Reciprocal and Quotient Identities
- Pythagorean Theorem Identities
- Cofunction Identities
- Odd-Even Identities
- Simplify Trigonometric Expressions using Identities
- Proving Trigonometric Identities
- Sum and Difference Identities
- Double-Angle
- Half-Angle Identities
- Product-Sum Identities
- Solving Trigonometric Equations

### Unit 7: Polar Coordinates & Parametric Equations

- Graphing Polar Coordinates
- Converting between Polar and Rectangular Coordinates
- Graphing Polar Equations
- Symmetry of Polar Graphs
- Identifying Classic Polar Curves
- Converting Equations Between Rectangular and Polar Form
- Graphing Complex Numbers
- Polar Form of Complex Numbers
- Multiplying and Dividing Complex Numbers
- DeMoivre's Theorem; Finding  $n^{\text{th}}$  Roots
- Graphing Parametric Equations
- Writing Parametric Equations in Rectangular Form
- Modeling with Parametric Equations

### Unit 8: Vectors

- Representing Vectors
- Magnitude and Direction of a Vector
- Component Form of a Vector
- Operations with Vectors
- Standard Unit Vector
- Linear Combinations
- Trigonometric Forms of Vectors
- Vector Applications
- Dot Products
- Orthogonal Vectors
- Vector Projections
- Force and Work Applications
- Vectors in Three-Dimensional Space

Unit 9: Conic Sections	Unit 10: Systems of Equations & Matrices
<ul style="list-style-type: none"> <li>• Graphing Circles</li> <li>• Writing Equations of Circles</li> <li>• Graphing Ellipses</li> <li>• Writing Equations of Ellipses</li> <li>• Graphing Hyperbolas</li> <li>• Writing Equations of Hyperbolas</li> <li>• Graphing Parabolas</li> <li>• Writing Equations of Parabolas</li> <li>• Applications of Conic Sections</li> <li>• General Conic Form</li> <li>• Classifying Conic Sections</li> <li>• Polar Forms of Conic Equations</li> </ul>	<ul style="list-style-type: none"> <li>• Linear Systems of Two-Variables Review: (graphing, substitution, and elimination methods)</li> <li>• Nonlinear Systems</li> <li>• Three-Variable Systems</li> <li>• Matrix Addition and Subtraction</li> <li>• Scalar Multiplication</li> <li>• Matrix Multiplication</li> <li>• Determinant of a Matrix</li> <li>• Inverse Matrices</li> <li>• Augmented Systems</li> <li>• Triangular Form for Linear Systems</li> <li>• Gaussian Elimination (row-echelon form)</li> <li>• Gauss-Jordan Elimination (reduced row-echelon form)</li> <li>• Solving Systems with Cramer's Rule</li> <li>• Solving Systems with Inverse Matrices</li> <li>• Partial Fractions</li> </ul>
Unit 11: Sequences, Series, & Induction	Unit 12: Introduction to Calculus
<ul style="list-style-type: none"> <li>• Sequences (Recursive &amp; Explicit)</li> <li>• Series &amp; Partial Sums</li> <li>• Summation Notation</li> <li>• Arithmetic Sequences</li> <li>• Arithmetic Series</li> <li>• Geometric Sequences</li> <li>• Geometric Series</li> <li>• Infinite Geometric Series</li> <li>• Mathematical Induction</li> <li>• The Binomial Theorem/Pascal's Triangle</li> </ul>	<ul style="list-style-type: none"> <li>• Finding Limits Graphically</li> <li>• One-Sided vs. Two-Sided Limits</li> <li>• Finding Limit Algebraically</li> <li>• Properties of Limits</li> <li>• Direct Substitution</li> <li>• Limits at Infinity</li> <li>• Limits of Sequences</li> <li>• Tangent Lines</li> <li>• Derivatives (using the definition)</li> <li>• Derivative Rules</li> <li>• Average Rate of Change/Velocity</li> <li>• Instantaneous Rate of Change/Velocity</li> </ul>